

Growth dynamics of complex business firms network

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In Japan there are about 1 million active business firms, and it is confirmed that the transaction relation network has a scale-free structure [1] and several non-trivial scaling relations are known to hold among quantities describing firm sizes such as annual sales, number of employees and number of business partners [2]. In view of network growth we find that annihilation, creation and merger are the key processes with the clear tendency of preferential attachment with higher link nodes, and stochastic simulation of these processes produces a complex network structure which reproduces the basic properties of real business network for the link number distribution [3]. We also show our new approaches to tune the frequency of 3-body motifs by revising the growth model [4]. Percolation properties [5] and anatomical decomposition [6] are applied to quantitative description of network structure in view of rigidity by removal of links wither randomly or intentionally.

Money flow on the whole network is approximated by a set of equations [7] that is based on the so-called the gravity law [8]. This set of equations is already implemented in RESAS (Regional Economy Society Analyzing System) [9], which is a big-data analysis platform provided by the government of Japan.

Acknowledgement: The data of business firms is provided for academic use by Teikoku Databank, which is the largest corporate credit research company in Japan.

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